

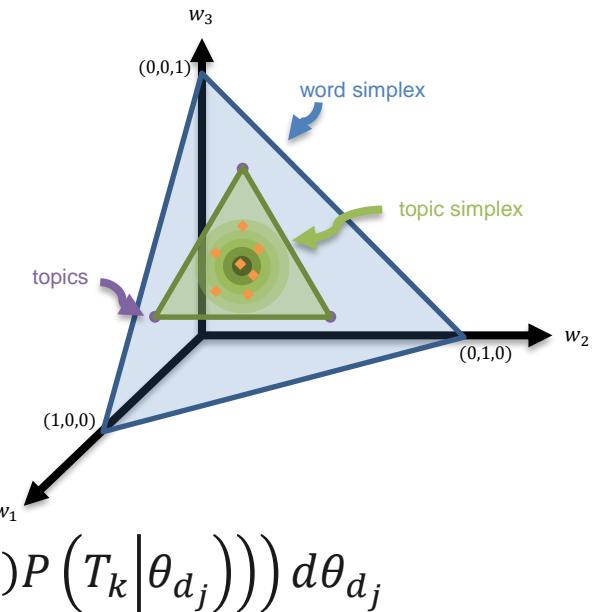
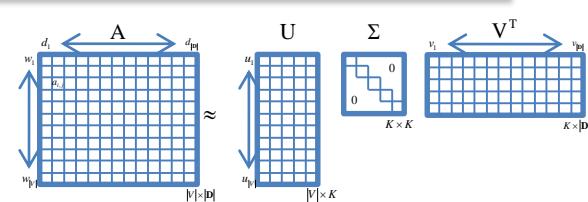
# Search Results Diversification

Kuan-Yu Chen (陳冠宇)

2020/11/20 @ TR-313, NTUST

# Review.

- Latent Semantic Analysis
  - Vector representation for word is  $\Sigma u_i^T$
  - Vector representation for document is  $\Sigma v_j^T$
- Statistical Topic Models
  - Probabilistic Latent Semantic Analysis
    - $\mathcal{L} = \prod_{w_i \in V} \prod_{d_j \in D} P(w_i, d_j)^{c(w_i, d_j)}$
  - Latent Dirichlet Allocation
    - $\mathcal{L} = \prod_{d_j \in D} \int P(\theta_{d_j} | \alpha) \left( \prod_{i=1}^{|d_j|} \left( \sum_{k=1}^K P(w_i | T_k, \beta) P(T_k | \theta_{d_j}) \right) \right) d\theta_{d_j}$



# Review..

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- The Expectation-Maximization algorithm
  - E-step

$$P(T_k | w_i, d_j) = \frac{P(w_i | T_k)P(T_k | d_j)}{\sum_{k=1}^K P(w_i | T_k)P(T_k | d_j)}$$

- M-step

$$P(w_i | T_k) = \frac{\sum_{d_j \in \mathbf{D}} c(w_i, d_j)P(T_k | w_i, d_j)}{\sum_{i'=1}^{|V|} \sum_{d_j \in \mathbf{D}} c(w_{i'}, d_j)P(T_k | w_{i'}, d_j)}$$

$$P(T_k | d_j) = \frac{\sum_{i=1}^{|V|} c(w_i, d_j)P(T_k | w_i, d_j)}{\sum_{i'=1}^{|V|} c(w_{i'}, d_j)} = \frac{\sum_{i=1}^{|V|} c(w_i, d_j)P(T_k | w_i, d_j)}{|d_j|}$$

- $P(w_i | T_k)$  and  $P(T_k | d_j)$  are random initial with two constraints
  - $\sum_{w_i \in V} P(w_i | T_k) = 1$ , for every topic  $T_k$
  - $\sum_{k=1}^K P(T_k | d_j) = 1$ , for every document  $d_j$

# Review...

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- About the M-step

$$\begin{aligned} P(w_i | T_k) &= \frac{c(w_i, T_k)}{\sum_{i'=1}^{|V|} c(w_{i'}, T_k)} \\ &= \frac{\sum_{d_j \in \mathbf{D}} c(w_i, T_k, d_j)}{\sum_{i'=1}^{|V|} \sum_{d_j \in \mathbf{D}} c(w_{i'}, T_k, d_j)} = \frac{\sum_{d_j \in \mathbf{D}} c(w_i, d_j) P(T_k | w_i, d_j)}{\sum_{i'=1}^{|V|} \sum_{d_j \in \mathbf{D}} c(w_{i'}, d_j) P(T_k | w_{i'}, d_j)} \end{aligned}$$

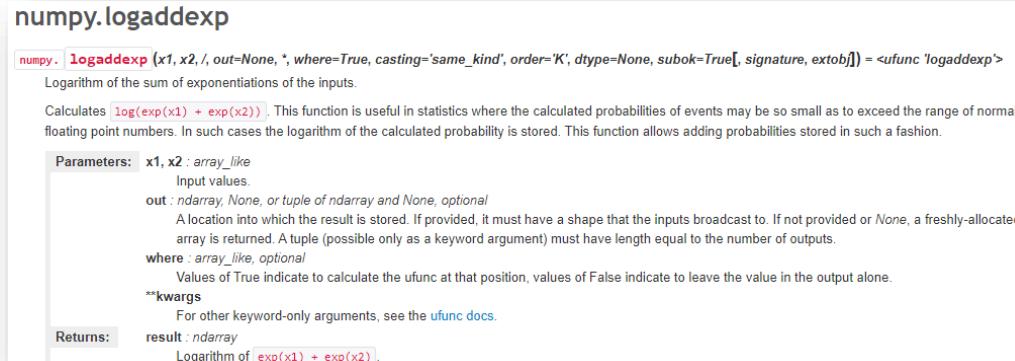
$$\begin{aligned} P(T_k | d_j) &= \frac{\sum_{i=1}^{|V|} c(w_i, d_j, T_k)}{\sum_{k'=1}^K \sum_{i'=1}^{|V|} c(w_{i'}, d_j, T_k)} \\ &= \frac{\sum_{i=1}^{|V|} c(w_i, d_j, T_k)}{\sum_{i'=1}^{|V|} c(w_{i'}, d_j)} \\ &= \frac{\sum_{i=1}^{|V|} c(w_i, d_j) P(T_k | w_i, d_j)}{\sum_{i'=1}^{|V|} c(w_{i'}, d_j)} = \frac{\sum_{i=1}^{|V|} c(w_i, d_j) P(T_k | w_i, d_j)}{|d_j|} \end{aligned}$$

# Review....

- The probability  $P(q|d_j)$  should be calculated in log domain

$$P(q|d_j) = \prod_{i=1}^{|q|} \left[ \alpha \cdot P(w_i|d_j) + \beta \cdot \left( \sum_{k=1}^K P(w_i|T_k)P(T_k|d_j) \right) + (1 - \alpha - \beta) \cdot P_{BG}(w_i) \right]$$

$$\begin{aligned} \log P(q|d_j) &= \sum_{i=1}^{|q|} \log \left[ \alpha \cdot P(w_i|d_j) + \beta \cdot \left( \sum_{k=1}^K P(w_i|T_k)P(T_k|d_j) \right) + (1 - \alpha - \beta) \cdot P_{BG}(w_i) \right] \\ &= \sum_{i=1}^{|q|} \left\{ [\log \alpha + \log P(w_i|d_j)] \oplus \left[ \log \beta + \log \left( \sum_{k=1}^K P(w_i|T_k)P(T_k|d_j) \right) \right] \oplus [\log(1 - \alpha - \beta) + \log P_{BG}(w_i)] \right\} \end{aligned}$$



# Homework 4.

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- The evaluation measure is MAP@1000
  - The **hard** deadline is 11/26 23:59
  - Your point is depended on your performance on the **private** leaderboard!
    - 50 public queries and 50 private queries

$$YourScore = 5 + \frac{YourMAP - BaselineMAP}{HighestMAP - BaselineMAP} \times 8$$

- Please submit a **report** and your **source codes** to the Moodle system, otherwise you will get 0 point
  - The report will be judged by TA, and the score is either 1 or 2

# Homework 4..

#	Team Name
1	宮澤賢治
2	康帕內魯拉
FYI: with 32 topics	
3	Test
4	M10815048_張晏銘
5	Enilesab
6	TESTT1235
7	B10615034_黃柏翰
8	Alice
9	80847002S_羅天宏
10	M10915100_郭智威
FYI: with 8 topics	
11	快樂ㄟ甘蔗man
12	hongyun
Baseline 0.4P(w D) 0.6P(w BG)	
13	在小世界裡畫出最耀眼的大幸福
14	trytrysee
15	騙人的吧

#	$\Delta$ pub	Team Name
1	▲ 1	康帕內魯拉
2	▲ 3	Enilesab
3	—	Test
4	—	M10815048_張晏銘
FYI: with 32 topics		
5	▼ 4	宮澤賢治
6	▲ 1	B10615034_黃柏翰
7	▲ 3	M10915100_郭智威
8	▼ 2	TESTT1235
9	—	80847002S_羅天宏
10	▼ 2	Alice
FYI: with 8 topics		
11	▲ 1	hongyun
12	▼ 1	快樂ㄟ甘蔗man
Baseline 0.4P(w D) 0.6P(w BG)		
13	—	在小世界裡畫出最耀眼的大幸福
14	—	trytrysee
15	—	騙人的吧

# About Final Project

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- Group your team!
  - 2~4 team members
  - Choose a paper
- Do you have GPU units?
  - We have to make sure you can do HW6 and/or final project

Date	Syllabus	Homework
9/18	<a href="#">Course Overview</a>	
9/25	Break for Roclng2020	
10/2	Holiday for Moon Festival	
10/9	Holiday for National Day	
10/16	<a href="#">Classic Models</a>	Homework-1(deadline: 10/29 23:59)
10/23	<a href="#">Extended Probabilistic Models</a>	Homework-2 (deadline: 11/5 23:59)
10/30	<a href="#">Evaluation &amp; Benchmark Collections</a>	<a href="#">Homework-3</a> (deadline: 11/12 23:59)
11/6	<a href="#">Latent Semantic Analysis</a>	
11/13	<a href="#">Statistical Topic Models</a>	Homework-4 (deadline: 11/26 23:59)
11/20	<a href="#">Search Results Diversification</a>	
11/27	<a href="#">Pseudo-Relevance Feedback &amp; Query Models</a>	<a href="#">Homework-5</a> (deadline: 12/10 23:59)
12/4	Talk	Submit Your Member List!
12/11	<a href="#">Representation Learning for Information Retrieval</a>	
12/18	<a href="#">Supervised Retrieval Models &amp; Information Retrieval in Practice</a>	<a href="#">Homework-6</a> (deadline: 12/31 23:59) & Submit Your Paper Title!
12/25	Break for Your Final Project	
1/1	Holiday for Founding Anniversary	
1/8	Presentation-1	
1/15	Presentation-2	

# Resource

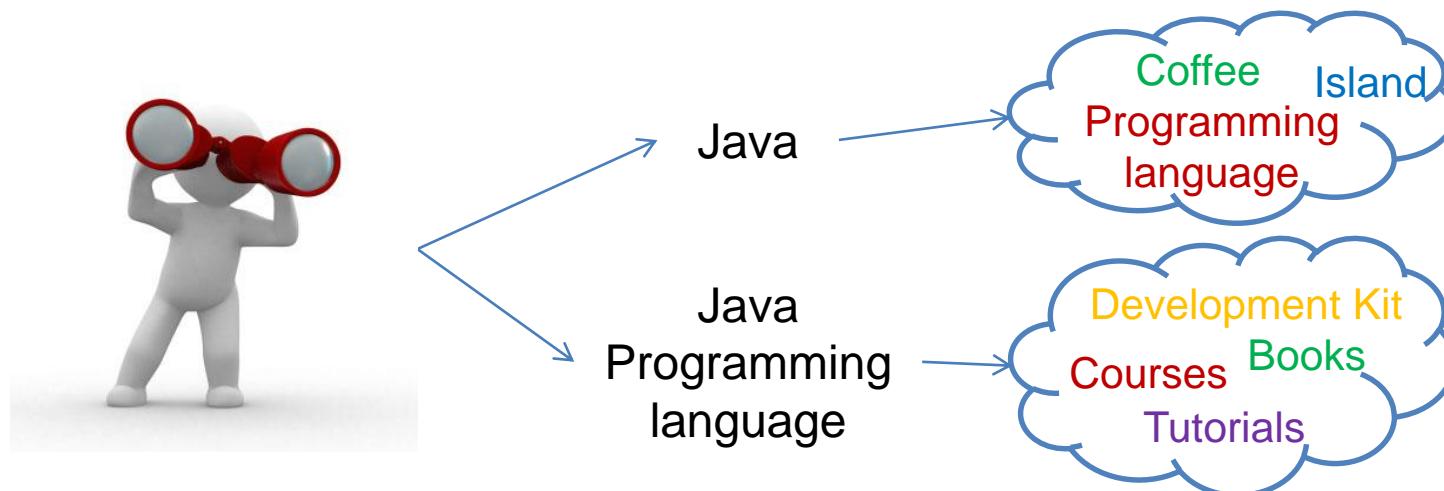
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- Conferences
  - ACM Annual International Conference on Research and Development in Information Retrieval (SIGIR)
  - International Joint Conferences on Artificial Intelligence (IJCAI)
  - ACM Conference on Information Knowledge Management (CIKM)
  - Annual Meeting of the Association for Computational Linguistics (ACL)
  - International Conference on Learning Representations (ICLR)
- Journals
  - Journal of the American Society for Information Science (JASIS)
  - ACM Transactions on Information Systems (TOIS)
  - Information Processing and Management (IP&M)
  - ACM Transactions on Asian Language Information Processing (TALIP)
  - Information Retrieval Journal (IRJ)

# Introduction – What's going on?

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- Traditional retrieval functions ignore the relations among returned documents
  - Top ranked documents may contain relevant yet **redundant information**
  - In order to maximize the satisfaction of different search users, it is necessary to diversify search results
  - Search results diversification can play an initial step for many search system



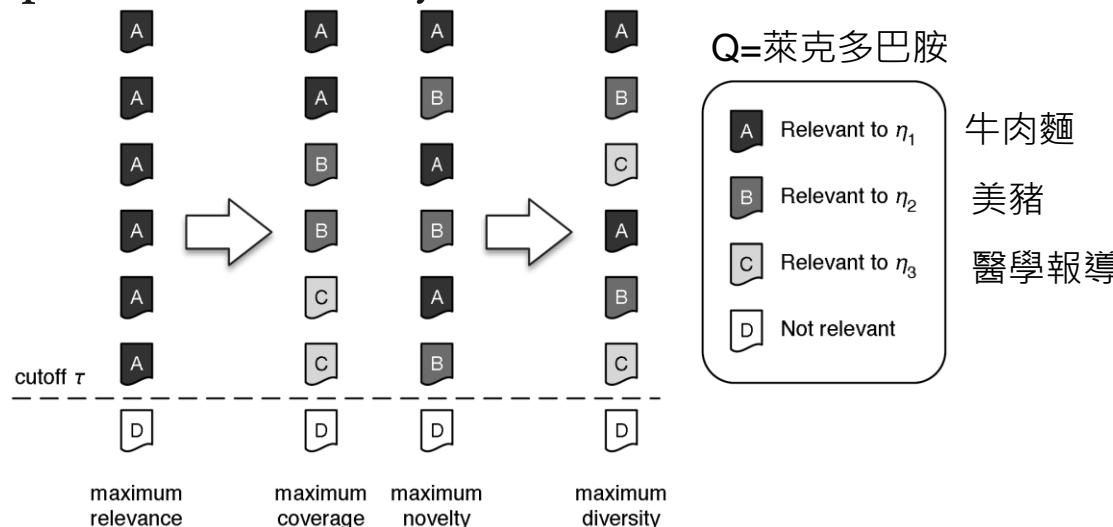
# Relevance, Coverage, Novelty, & Diversity

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- Most of the retrieval models assume that the relevance of a document can be estimated with **certainty** and **independently** of the estimation of the other retrieved documents
  - Ambiguous queries
    - Ensuring a high **coverage** of the possible information needs
  - Redundancy results
    - Ensuring the retrieved documents provide a high **novelty**

# Relevance, Coverage, Novelty, & Diversity

- Coverage and novelty can be conflicting objectives
  - A ranking with maximum coverage may not attain maximum novelty
    - Although covering all information needs, the ranking may place all documents covering a particular need ahead than others
  - A ranking with maximum novelty may not attain maximum coverage
    - Although covering each need as early as possible in the ranking, not all possible needs may be covered



# Example.

Google 萊克多巴胺

約有 3,030,000 項結果 (搜尋時間 : 0.37 秒)

廣告 · www.twreporter.org/ ▾

**綜合報導**

美豬美牛的10大爭議 - 瘦肉精是什麼？安全嗎？

食安風險未明的萊克多巴胺，歐盟至今仍維持禁令，瘦肉精對人體有無危害？美國為何不斷要求開放？對台灣畜牧產業又會有什麼影響？《報導者》整理出10大爭議，解析全面開放美豬牛的影響。類型：深度在地報導，開啟新聞革命，非營利媒體。

zh.wikipedia.org, zh-tw, 萊克多巴胺 ▾

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萊克多巴胺 (Ractopamine) 是一種β促效劑 (β-agonist) 藥物，用以助長豬、牛、火雞生出瘦肉，減少體脂肪。是瘦肉中最常見的一種，其肉品殘留毒性遠低於 ...

化學定義

化學式：C<sub>18</sub>H<sub>23</sub>NO<sub>3</sub>  
CAS號：97825-25-7  
瘦肉精 · 臺灣進口美國牛肉問題 · 雙盲

溶解性 (水)：4100 mg/L  
SMILES：显示▼: OC(c1ccc(O)cc1)CNC(=O)C(C)CCc2ccc(O)cc2

www.businessweekly.com.tw, 焦點，時事分析 ▾

**周刊科普**

萊克多巴胺有多可怕？別讓「不了解」蒙蔽了判斷力 | 商周

2020年9月17日 — 然而萊克多巴胺究竟是什麼？這其實是歷經多年嚴謹研究，為了提升牲口肉品產量與安全使用所發展而成的飼料添加物，可減少飼料用量 ...

health.tvbs.com.tw, 營養 ▾

瘦肉精是什麼？吃了含萊克多巴胺的豬肉會怎樣？有方法排毒嗎 ...

2020年8月31日 — 政府宣布明年1月1日起，將放寬含瘦肉精的美豬美牛進口，引起國人恐慌。台北榮民總醫院臨床毒物與職業醫學科主任楊振昌提醒，萊克多巴胺是 ...

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Taiwan News · 1 天前

萊克多巴胺

萊克多巴胺是一種β促效劑藥物，用以助長豬、牛、火雞生出瘦肉，減少體脂肪。是瘦肉中最常見的一種，其肉品殘留毒性遠低於具有相同功能的其他動物飼料添加物。美國謊稱在其測定的容許殘留量下合法使用，將不會對人類造成中毒或短期危害。目前的實驗數據確定會對人體產生其他副作用，人體長期攝取殘留的萊克多巴胺會造成健康問題！維基百科

分子式：C<sub>18</sub>H<sub>23</sub>NO<sub>3</sub>  
PubChem CID：56052  
溶解性 (水)：4100 mg/L  
化學式：C<sub>18</sub>H<sub>23</sub>NO<sub>3</sub>  
CAS號：97825-25-7  
SMILES：顯示▼: OC(c1ccc(O)cc1)CNC(=O)C(C)CCc2ccc(O)cc2

其他人都搜尋了

Tretoquinol 偶氮甲醯胺 Procaterol

意見回饋

# Example..

Google 蘋果

全部 新聞 圖片 地圖 影片 更多 設定 工具

約有 147,000,000 項結果 (搜尋時間 : 0.50 秒)

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營業時間 ▾

**A 銘電科技有限公司(蘋果專門店)-文山專業ipad維修|專業iphon...**  
台北市文山區 · 02 2930 1930  
已打烊 · 開始營業時間 : 12:00

**B Apple 台北101**  
台北101  
台北市信義區 · 02 8726 3500  
已打烊 · 開始營業時間 : 11:00  
✓ 來店取貨

**C Apple Shop 煙坤和平店**  
台北市中正區 · 02 2327 8336  
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蘋果公司 (英語：Apple Inc.)，原稱蘋果電腦公司 (英語：Apple Computer, Inc.)，是總部位於美國加州庫比蒂諾的跨國科技公司，與亞馬遜、谷歌、微软 ...  
創辦人：史蒂夫·乔布斯; 斯蒂夫·沃茲尼亞克; ... 營業額：▼ 2601.74億美元 (2019)  
總資產：▼ 3385.16億美元 (2019) 成立：1976年4月1日，44年前

zh.wikipedia.org › zh-tw › 苹果 ▾

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苹果，又稱柰或林檎，是苹果樹 (学名：*Malus pumila*) 的果实。苹果樹是薔薇科苹果亞科苹果属植物，為落叶乔木，果实富含矿物质和维生素，是人们最常食用的 ...  
科：薔薇科 Rosaceae 界：植物界 Plantae  
种：苹果 *M. pumila* 属：苹果属 Malus

m.momoshop.com.tw › 品牌旗艦 › Apple ▾

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Apple, 品牌旗艦, iPhone, iPad, Mac 優惠便宜好價格！Apple 蘋果 品牌推薦，並提供您完整規格種類的 iPhone, iPad, Mac !

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**不僅效能IBM說出蘋果拋棄Intel處理器真相| XFastest News**  
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news.cnyes.com › 國際股 › 美股 ▾

**投行提證據！iPhone 12 正啟動蘋果超級週期| Anue鉅亨- 美股**  
7 小時前 — 相信這將轉化為蘋果前所未有的升級週期。週四Daniel Ives 重申其觀點。蘋果十月中旬發布四款新iPhone 12，包括5.4吋iPhone 12 Mini、6.1吋 ...

technews.tw › 2020/11/18 › app-store-2 ▾

**蘋果調降App Store一半佣金，營收百萬美元以下小企業受惠 ...**  
2 天前 — 蘋果 (Apple) 的App Store 付費App 與App 內購佣金一向為許多開發者所詬病，因為每次Apple 都會抽佣30%；尤其今年疫情橫行，對於許多 ...

# Introduction – Various Modeling

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- Many diversification methods have been proposed
  - balance the relevance and the redundancy: MMR
  - distinguish previous topics and new coming: SMM
  - language modeling approach: WUME
  - probabilistic framework: xQuAD
- These methods mainly differ in **diversity modeling**
  - **Implicitly**: The diversity is implicitly modeled through document similarities
  - **Explicitly**: It can be explicitly modeled through the coverage of query subtopics, and document dependency

# Introduction – Notations

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Symbol	Description
$q$	A given query
$a_k^q$	Sub-queries (aspect), $q = \{a_1^q, \dots, a_K^q\}$
$K$	Number of sub-queries
$R$	The user's information need
$\mathbf{D}$	A set of documents, $\mathbf{D} = \{d_1, \dots, d_{ \mathbf{D} }\}$
$\tilde{\mathbf{D}}$	A subset of documents which already selected by new method, $\tilde{\mathbf{D}} = \{\tilde{d}_1, \dots, \tilde{d}_{ \tilde{\mathbf{D}} }\}$

# Maximal Marginal Relevance – MMR

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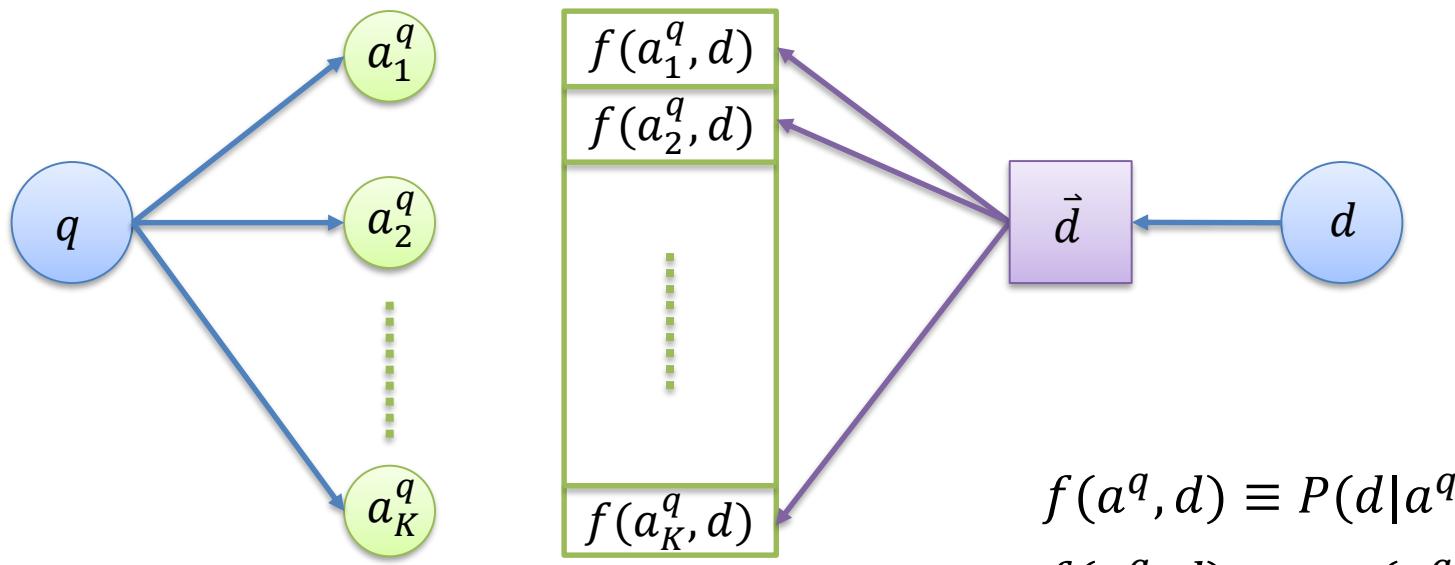
- MMR motivated the need for “relevant novelty” as a potentially superior criterion
  - An approximation to measuring relevant novelty is to **measure relevance and novelty independently**
- “Marginal Relevance” can be regarded as the metric
  - A document has high **marginal relevance** if it is both relevant to the query and contains minimal similarity to previously selected documents

$$Div_{MMR}(d, q) = - \max_{\tilde{d} \in \tilde{\mathbf{D}}} sim(d, \tilde{d})$$

$$score(d, q) = \lambda \cdot Rel(d, q) - (1 - \lambda) \cdot \max_{\tilde{d} \in \tilde{\mathbf{D}}} sim(d, \tilde{d})$$

# Explicit MMR – xMMR

- For a given query with its sub-queries, each document can be represented by a  $K$ -dimensional vector over sub-queries



- By doing so, the redundancy score can be defined by considering sub-queries

$$score(d, q) = \lambda \cdot Rel(d, q) - (1 - \lambda) \cdot \max_{\tilde{d} \in \tilde{\mathcal{D}}} sim(d, \tilde{d})$$

# Simple Mixture Model – SMM

- Given the observed new document, we estimate the mixing weight for the background model  $\theta_{BG}$  and the previous topic model  $\theta_T$ 
  - The simplest previous topic model can be modeled as:

$$P(w|\theta_T) = \sum_{\tilde{d} \in \tilde{\mathbf{D}}} \frac{1}{N} P(w|\tilde{d})$$

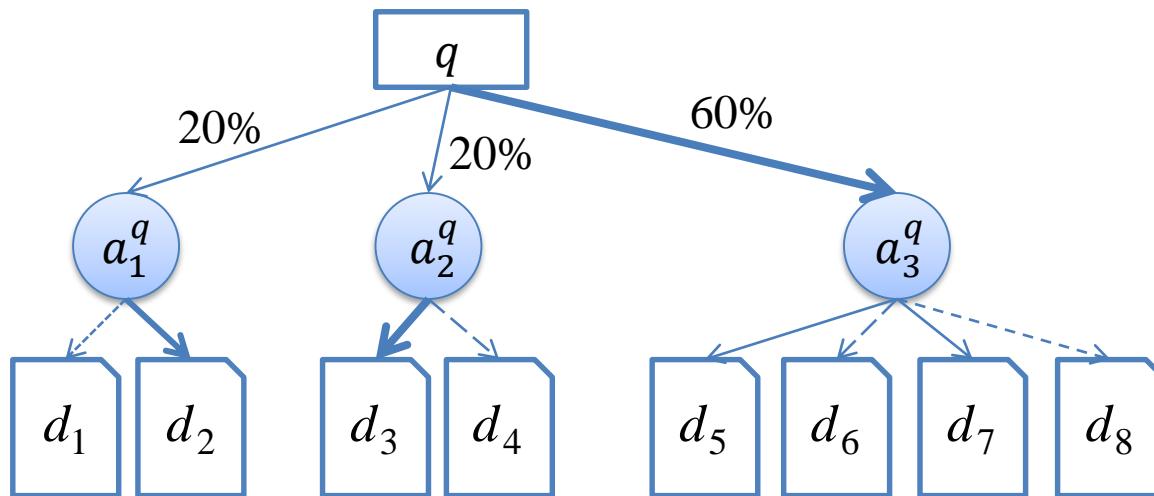
- The mixture weight for the background model can serve as a measure of novelty or redundancy

$$L(\beta|d, \theta_{BG}, \theta_T) = \prod_{w \in V} ((1 - \beta) \cdot P(w|\theta_T) + \beta \cdot P(w|\theta_{BG}))^{c(w,d)}$$

$$L(\beta|d, \theta_{BG}, \theta_T) = \prod_{w \in V} (P(\theta_T|d) \cdot P(w|\theta_T) + P(\theta_{BG}|d) \cdot P(w|\theta_{BG}))^{c(w,d)}$$

$$score(d, q) = \lambda \cdot Rel(d, q) + (1 - \lambda) \cdot \beta$$

# WUME – Motivation



- There are three sub-queries under the given query  $q = \{a_1^q, a_2^q, a_3^q\}$ , and web documents  $\mathbf{D} = \{d_1, \dots, d_8\}$
- Although  $d_3$  is more relevant to one of the sub-query  $a_2^q$  than  $d_5$  to  $a_3^q$ , given that  $a_2^q$  attracts less user interest than  $a_3^q$ ,  $d_3$  should still be **ranked lower** than  $d_5$

# WUME

- WUME formalize the diversification method as:
  - Given a query  $q$ , the probability that a retrieved document meets user's information need  $R$  can be written as:

$$P(R|d) = \frac{P(R)P(d|R)}{P(d)} \propto P(d|R)$$

- Take sub-query information into consideration:

$$P(d|R) \approx P(d|q) = \sum_{k=1}^K P(d|a_k^q, q)P(a_k^q|q)$$

Google Insights for  
Search or Wikipedia

- Finally, the ranking function becomes:

$$score(d, q) = \lambda \cdot Rel(d, q) + (1 - \lambda) \cdot \sum_{k=1}^K P(d|a_k^q, q)P(a_k^q|q)$$

The screenshot shows a Wikipedia page for the topic 'LDA'. The sidebar on the left contains a 'Main page' link, a 'Contents' link, and a 'Recent events' link. Below these are links for 'Random article', 'About Wikipedia', 'Contact us', and 'Donate'. Further down are links for 'Contribute', 'Help', 'Learn to edit', 'Community portal', 'Recent changes', and 'Upload file'. The 'Tools' section includes links for 'What links here', 'Related changes', 'Special pages', 'Permanent link', 'Page information', 'Cite this page', and 'Wikidata item'. Under 'Print/export', there are links for 'Download as PDF' and 'Printable version'. The 'Languages' section lists 'Deutsch', 'Español', 'Français', '한국어', '日本語', 'Türkçe', and '中文', with a link to '4 more'. The main content area lists several topics under 'LDA' with a blue 'edit' link next to each. Some topics are underlined, such as 'Latent Dirichlet allocation' and 'Lobbying Disclosure Act of 1995'. The 'Aviation' section lists 'Localizer type directional aid' and 'Landing distance available'. The 'Law' section lists 'Legal document assistant' and 'Lobbying Disclosure Act of 1995'. The 'Medicine' section lists 'Left-displaced abomasum' and 'Low dose allergens'. The 'Science and technology' section lists 'Laser Doppler anemometry', 'Latent Dirichlet allocation', 'Linear discriminant analysis', 'Lithium diisopropylamide', 'Local delivery agent', 'Local-density approximation', 'Low density amorphous ice', and 'Lobate debris apron'. The 'Organizations' section lists 'Lahore Development Authority', 'Liga Deportiva Alajuelense', 'London Democratic Association', and 'London Development Agency'.

# eXplicit Query Aspect Diversification

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- xQuAD: eXplicit Query Aspect Diversification
  - When given an ambiguous query, xQuAD estimates the ranking score by:

$$score(d, q) = \lambda \cdot P(d|q) + (1 - \lambda) \cdot P(d, \bar{\mathbf{D}}|q)$$

- $P(d|q)$  is the likelihood of document  $d$  being observed given the initial query

The probability can be regarded as modeling *relevance*
- $P(d, \bar{\mathbf{D}}|q)$  is the likelihood of observing this document but not the documents already in  $\bar{\mathbf{D}}$ 

The probability can be regarded as modeling *diversity*

# xQuAD – 1

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- In order to derive  $P(d, \bar{\mathbf{D}}|q)$ , xQuAD explicitly consider the possibly several aspects underlying the initial query as a set of sub-queries

- By assuming  $\sum_{k=1}^K P(a_k^q|q) = 1$ , xQuAD calculates  $P(d, \bar{\mathbf{D}}|q)$  by considering sub-queries:

$$P(d, \bar{\mathbf{D}}|q) = \sum_{k=1}^K P(d, \bar{\mathbf{D}}|a_k^q) P(a_k^q|q)$$

- Further,  $P(d, \bar{\mathbf{D}}|a_k^q)$  can be broken down by independent assumption:

$$P(d, \bar{\mathbf{D}}|a_k^q) = P(d|a_k^q) P(\bar{\mathbf{D}}|a_k^q)$$

*coverage*      *novelty*  
↓              ↓

## xQuAD – 2

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- For  $P(\bar{\mathbf{D}}|a_k^q)$ , xQuAD assumes that the relevance of each document in  $\bar{\mathbf{D}}$  to a given sub-query  $a_k^q$  is independent

$$P(\bar{\mathbf{D}}|a_k^q) = P(\tilde{d}_1, \dots, \tilde{d}_{|\bar{\mathbf{D}}|} | a_k^q) = \prod_{\tilde{d}_n \in \bar{\mathbf{D}}} P(\tilde{d}_n | a_k^q) = \prod_{\tilde{d}_n \in \bar{\mathbf{D}}} (1 - P(\tilde{d}_n | a_k^q))$$

- To sum up, xQuAD suggests that:

$$\begin{aligned} P(d, \bar{\mathbf{D}} | q) &= \sum_{k=1}^K P(d, \bar{\mathbf{D}} | a_k^q) P(a_k^q | q) \\ &= \sum_{k=1}^K P(a_k^q | q) P(d | a_k^q) P(\bar{\mathbf{D}} | a_k^q) \\ &= \sum_{k=1}^K P(a_k^q | q) P(d | a_k^q) \prod_{\tilde{d}_n \in \bar{\mathbf{D}}} (1 - P(\tilde{d}_n | a_k^q)) \end{aligned}$$

# xQuAD – 3

- The final score for each document is determined by:

$$\begin{aligned} score(d, q) &= \lambda \cdot P(d|q) + (1 - \lambda) \cdot P\left(d, \bar{\mathbf{D}}|q\right) \\ &= \lambda \cdot P(d|q) + (1 - \lambda) \cdot \sum_{k=1}^K \underbrace{P(a_k^q|q)P(d|a_k^q)}_{\text{the importance of } a_k^q} \prod_{\tilde{d}_n \in \bar{\mathbf{D}}} (1 - P(\tilde{d}_n|a_k^q)) \end{aligned}$$

the importance of  $a_k^q$

the relevance of  $d$  to  $a_k^q$

the satisfaction degree  $a_k^q$

- Instead of comparing a document  $d$  to all documents already selected in  $\bar{\mathbf{D}}$ , xQuAD estimates the utility of any document satisfying the sub-query  $a_k^q$ , given how well it is already satisfied by the documents in  $\bar{\mathbf{D}}$

# Analytical Comparisons

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- Diversity Modeling:
  - MMR and SMM **implicitly** model the diversity through document similarities
  - xMMR, WUME and xQuAD **explicitly** model the diversity through the coverage of query subtopics
- Document Dependency:
  - WUME assumes that the diversity score of a document is independent of other documents
  - The other three methods assume that the diversity score depends on the previously selected documents

# General Framework

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- Most of these methods **iteratively select** the document that is not only **relevant** to the query but also **diversified** to cover more query subtopics, explicitly or implicitly
- All of methods fit into a general framework that iteratively selects with the highest relevance and diversity scores:

$$d^* = \operatorname{argmax}_{d \in \mathbf{D}} \lambda \cdot \text{Rel}(d, q) + (1 - \lambda) \cdot \text{Div}(d, q)$$

# Experimental Results

	TREC09 result		TREC10 result	
	$\alpha$ -nDCG@20	$\alpha$ -nDCG@100	$\alpha$ -nDCG@20	$\alpha$ -nDCG@100
$MMR^*$	0.365	0.427	0.344	0.415
$WUME^*$	0.479	0.546	0.579	0.630
$xQuAD^*$	0.482	0.550	0.588	0.636

- All the parameters in each method are set to the optimum values
  - Both xQuAD and WUME perform significantly better than MMR
    - Using explicit sub-queries in diversification is better
    - The performances of xQuAD and WUME are not significantly different

# Conclusions

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- The experiment result shows that the explicit sub-query modeling and sub-query importance penalization strategies perform better
- It is interesting to find that how the sub-queries affect the overall performance
- Finally, we can think about that what's the difference between sub-queries and latent topics?
  - Supervised v.s. Unsupervised?
- Beyond relevance? Another relevance?

$$P(d|R) \approx P(d|q) = \sum_{k=1}^K P(d|a_k^q, q)P(a_k^q|q)$$

# Questions?

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